

RIGID FRAME STUDIES

Progress Report

DESIGN METHODOLOGY FOR TAPERED BEAMS

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INTRODUCTION

In a previous report (1), differential equations for elastic, singly symmetrical, laterally unbraced, web-tapered members subjected to unequal end moments were derived using the energy approach suggested by Trahair and his research team (2,3,4). The differential equations were solved by the Rayleigh-Ritz procedure to find the critical moments. Solutions were verified with a finite element method and by comparison with available closed-form solutions for prismatic members. For design purposes, modifying coefficients for prismatic beam solutions to account for taper and moment gradient were developed using a multiple linear regression technique. The developed simplified procedure was found to be accurate to $\pm 8\%$ for tapered beams in single curvature, and $\pm 12\%$ for double curvature.

The present report further develops the proposed design methodology. The elastic results are extended to the inelastic range using the CRC formula (5):

$$\sigma_{cr} = \sigma_y - \frac{\sigma_y^2}{4\sigma_e} \quad (1)$$

where σ_{cr} = inelastic buckling stress, σ_y = yield stress, and σ_e = elastic buckling stress. Ultimate load is defined by

either elastic or inelastic lateral-torsional buckling or by first yield when residual stresses are neglected. These are the same criteria as the allowable stress design procedures of the AISC specification (6).

To facilitate computational efficiency a small computer program was developed and is described. Manual solutions for a wide range of problems are presented for verification of the computer program.

DESIGN METHODOLOGY FOR TAPERED BEAMS

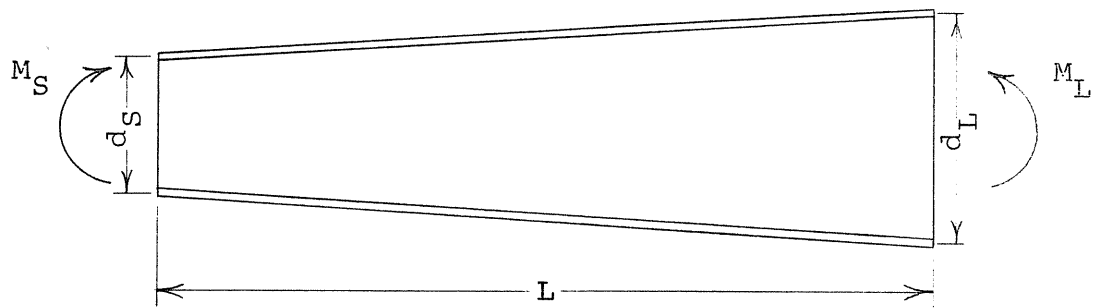
The design methodology used for web-tapered beams subjected to end moments, Figure 1a, is based on solutions for a prismatic beam with the same cross-section as at the small end of the tapered beams and subjected to equal but opposite end moments as shown in Figure 1b. This beam and loading condition is referred to as the "basic case" prismatic beam. For singly symmetrical cross-sections loaded in the plane of symmetry, the elastic critical moment for the basic case is

$$M_e = \pm \frac{\pi^2 EI_y \beta_x}{2L^2} \left\{ 1 + \sqrt{1 + \frac{4}{\beta_x^2} \left(\frac{C_w}{I_y} + \frac{GJL^2}{\pi^2 EI_y} \right)} \right\} \quad (2a)$$

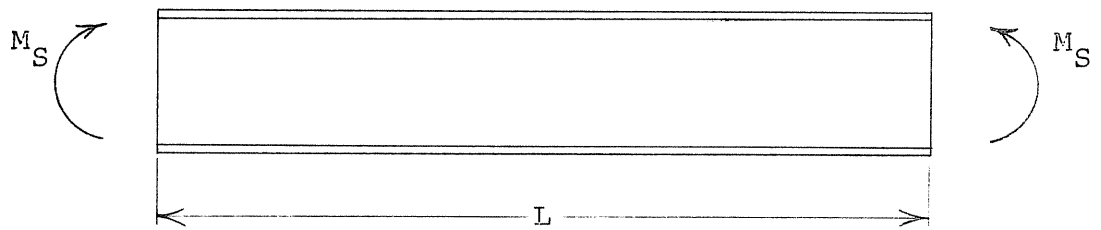
where I_y = weak axis moment of inertia, β_x = a cross-sectional property to be defined later, L = unbraced length of the tapered beam, C_w = warping moment of inertia, J = torsion constant, E = modulus of elasticity, and G = shear modulus of elasticity. The positive root is taken when the large flange is in compression; the negative root is taken when the small flange is in compression.

For doubly symmetrical sections β_x is zero and equation 2a reduces to

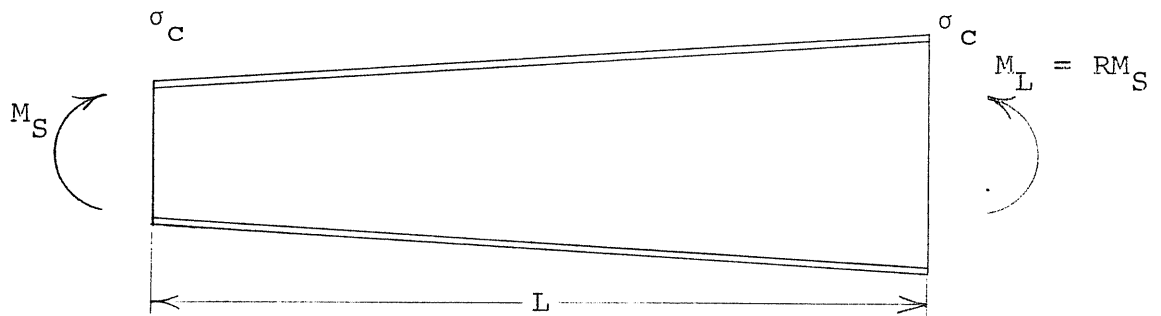
$$M_e = \pm \frac{\pi^2}{2L^2} \sqrt{EI_y GJ + \frac{E^2 I_y C_w \pi^2}{L^2}} \quad (2b)$$



a) Tapered Beam Subjected to End Moments



b) Basic Case Prismatic Beam



c) Basic Case Tapered Beam

Figure 1. Beam Geometry and Loading

The tapered beam basic case loading condition is defined as equal compressive stress at the exterior flange tips when the beam is bent in single curvature as shown in Figure 1c. This loading condition produces approximately uniform compressive flange stress along the member. The relationship between end moments is

$$M_S = R M_L \quad (3)$$

where M_S = moment at small end, M_L = moment at large end, and R = the ratio of the section moduli to the extreme fiber of the compression flange at the large end to that at the small end.

The critical moment for the tapered beam, basic case loading, is estimated from

$$(M_e)_S = C_a M_e \quad (4)$$

where M_e is determined from equations 2a or 2b, (M_e) = the critical moment at the small end of the tapered beam and C_a = a coefficient to account for the effects of taper. The critical moment at the large end for the basic case loading is

$$(M_e)_L = R (M_e)_S = R C_a M_e \quad (5)$$

For the case of varying flange stress along the member, Figure 1a, equations 4 and 5 are modified to

$$(M_e)_S = C_b C_a M_e \quad (6a)$$

$$(M_e)_L = C_b R C_a M_e \quad (6b)$$

where C_b is a modifying factor to account for stress variation due to unequal compressive flange stresses at the beam ends.

The multiplying factors C_a and C_b were determined using multiple linear regression analysis of theoretically correct values of critical moments for tapered beams (1). The best-fit equation for C_a is

$$C_a = 1.0 - 1.4580 \alpha \sqrt{\frac{GJL^2}{EC_w} + 44.6328} \alpha \frac{J}{I_y} \quad (7)$$

Here

$$\alpha = \frac{d_L - d_S}{L}$$

where d = beam depth.

The multiplying factor C_b depends on the relative stresses in a flange at each end of the beam. Defining "r" as the stress ratio such that

$$-1.0 \leq r = \frac{\sigma_{opp}}{\sigma_{max}} \leq 1.0$$

where σ_{max} is the maximum compressive flange stress at a beam end and σ_{opp} is the stress in the same flange at the opposite end of the beam. A stress ratio of +1.0 is equivalent to the tapered beam basic case loading, e.g. single curvature, and a ratio of -1.0 is equivalent to double curvature bending with stresses in the reference flange equal in magnitude but opposite in sense at opposite ends. It was not possible to find a single best-fit equation for C_b over the entire stress ratio range. For stress ratios greater than -0.40, C_b is

given by

$$C_b = 1.0 - 0.3867(r-1.0) + 0.4739(r-1.0)^2 + 0.9074 \frac{\alpha L}{d}(r-1)^2 \quad (8)$$

Best-fit equations for the range $-0.40 > r \geq -1.0$ predicted unacceptable unconservative results. An acceptable design approach for this range is to compute C_b for $r = -0.40$ from equation 8 and C_b for $r = -1.0$ from

$$C_b = 2.7596 - 2.8152 \frac{\beta x}{d} - 0.6562 \frac{\alpha L}{d} - 15.6530 \alpha \frac{\beta x}{d} \quad (9a)$$

for small end reference and

$$C_b = 2.7684 + 1.2025 \frac{\alpha L}{d} - 2.2686 \frac{\beta x}{d} - 22.0724 \alpha \frac{\beta x}{d} \quad (9b)$$

for large end reference and use linear interpolation between the two values to determine C_b for the given r .

If the resulting value of M_e is greater than $0.5M_y$ for the referenced flange the CRC formula, equation 1, is to be used to estimate the inelastic critical moment, M_{cr} . A check must also be made to determine if the tension flange yields.

The equations for C_a and C_b are applicable only to cross-sections, taper ratios and unbraced lengths normally found in rigid frames of pre-engineered metal buildings and the following limitations must be followed:

$$\begin{array}{ll} 1.5 \leq \frac{\text{minimum depth}}{\text{flange width}} \leq 3.0 & 6 \text{ in.} \leq d_L \leq 24 \text{ in.} \\ 24 \geq \frac{\text{span length}}{\text{minimum depth}} & 3 \text{ in.} \leq \text{flange width} \leq 12 \text{ in.} \\ 15 \leq \frac{\text{flange width}}{\text{flange thickness}} \leq 50 & \frac{3}{16} \text{ in.} \leq \text{flange thickness} \leq \frac{3}{4} \text{ in.} \end{array}$$

In addition, to limit the unconservative error to less than 8% for beams in single curvature and to less than 12% for beams in double curvature, both at the 95% confidence level, in the range $-0.4 \geq r \geq 1.0$, the following limitations must be observed

$$\frac{I_{yL}}{I_{yS}} \left(\frac{\alpha L}{d} \right) \leq 1.30 \qquad \frac{I_{yL}}{I_{yS}} \leq 2.5$$

It is noted that the error of estimation is reduced as the taper decreases and as the cross-section becomes more nearly doubly symmetric.

The design procedure is summarized as follows:

- (1) For a given member and end moments, calculate the extreme fiber compressive stresses at the beam ends. The flange location with the largest stress is chosen as the reference end flange
- (2) Calculate the basic case critical moment for a prismatic beam with the same cross-section as the small end of the beam in question and with the flange corresponding to the reference flange in compression, using either equation 2a or 2b.
- (3) Calculate the modifying factor C_a with reference to the small end section properties, using equation 7.
- (4) Calculate the stress ratio, r , as the ratio of the beam end stresses in the reference flange. Note that r is greater than zero for single curvature bending and less than zero for double curvature

bending.

- (5) If r is greater than -0.40 , use equation 8 and the referenced end properties to calculate C_b .
- (6) If r is less than -0.40 , calculate C_b for $r = 0.40$ using equation 8 and C_b for $r = -1.0$ using equation 9a for small end reference and 9b for large end reference. Use linear interpolation between these two value to determine C_b for the stress ratio in question.
- (7) Calculate R , the ratio of section moduli to extreme fibers of the reference flange at the beam ends.
- (8) Calculate the tapered beam critical moments using equation 6a for small end reference and equation 6b for large end reference.
- (9) Determine if the critical moment exceeds one-half of the first yield moment of the referenced flange. If this moment is exceeded, estimate the inelastic critical moment using equation 1.
- (10) Determine the critical moment at the opposite end using equation 3.
- (11) Check that the yield stress of the material is not exceeded in the tension flanges. If it is, reduce the moment to a value which causes first yield in the tension flange and use equation 3 to determine the moment at the opposite end.
- (12) Apply a factor of safety, commonly 1.67, to obtain the working load moments.

A flow chart of the procedure is shown in Figure 1 in terms of stresses rather than moments. A listing of a FORTRAN IV computer program for the design procedure is found in the appendix to this report. The sign convention for moments in this program is clockwise moments are positive.

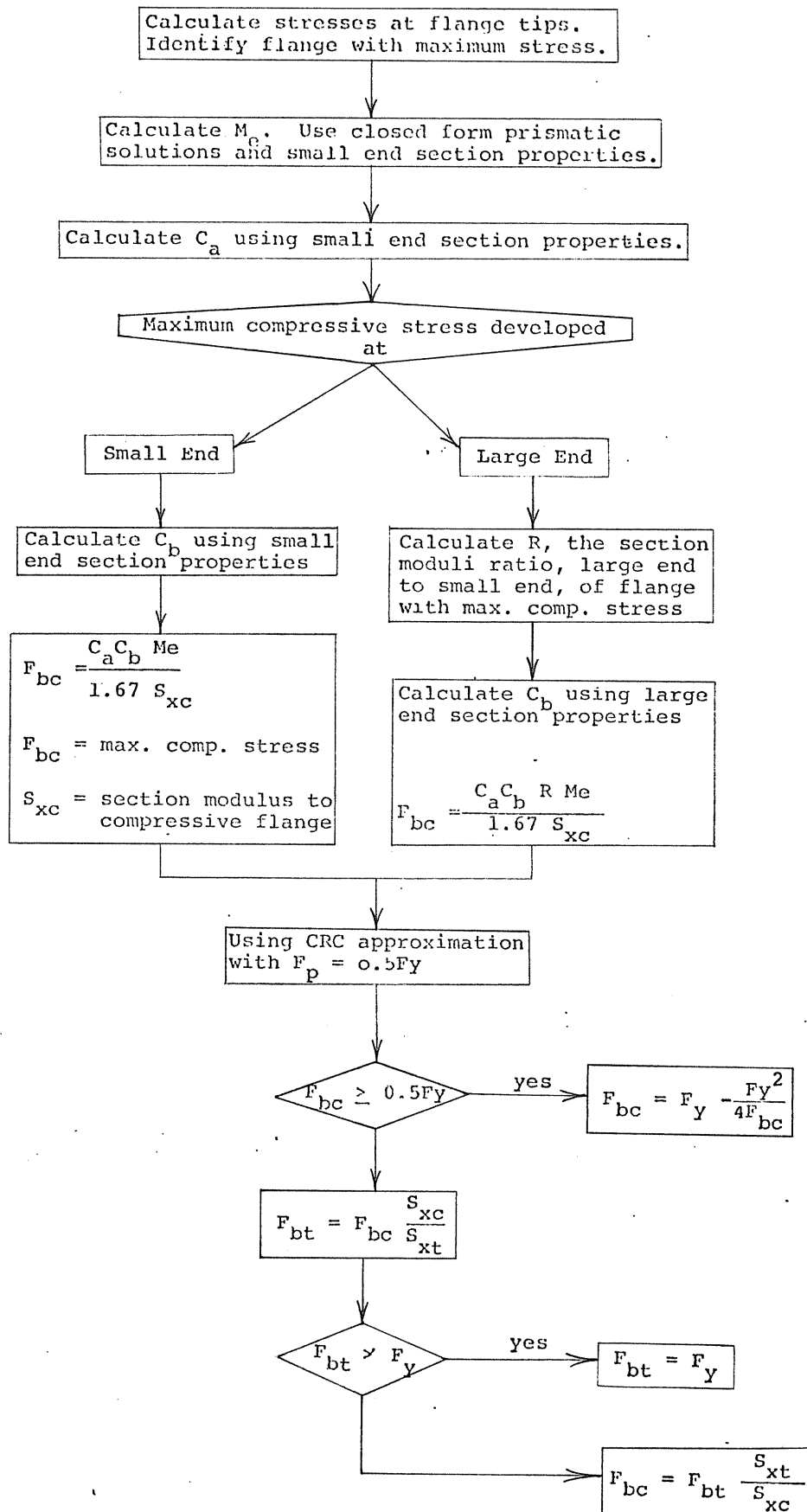
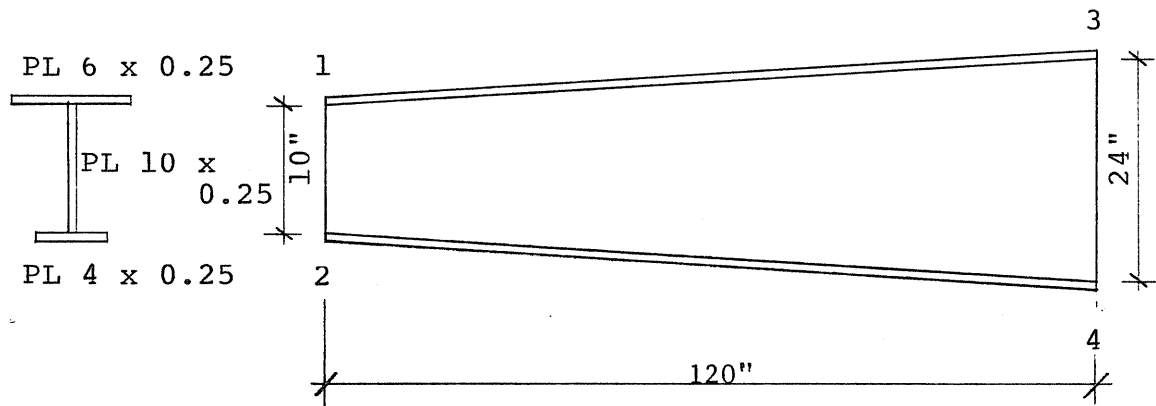


Figure 2. Flow Chart for Design Procedure

EXAMPLE CALCULATIONS

The singly symmetrical, laterally unbraced, tapered beam shown in Figure 3 was analyzed manually to determine the critical moments and stresses for the four loadings shown in Figure 4. The results from the computer program are found in the Appendix and are identical to the manual calculations.

In the calculations that follow, flange tips are referenced as shown in Figures 3 and 4. For each loading case the stresses at the four flange extremities are first calculated, and the reference end and reference flange determined. Next the prismatic elastic buckling moment is found and the modifying factors to account for taper and stress gradient determined. The elastic buckling stress for the critical location is then calculated and compared to the assumed proportional limit ($0.5 F_y$). If the elastic buckling stress exceeds the proportional limit, the inelastic buckling stress is estimated using the CRC formula. Once the critical stress is found, the stress in the tension flange is computed and compared to the yield stress. If the yield stress is exceeded, the corresponding moments at each end are computed. Finally, stresses caused by the final moments are calculated.



$$\alpha = \frac{24 - 10}{120} = 0.1167 \quad E = 30,000 \text{ ksi}$$

$$F_y = 50.0 \text{ ksi} \quad G = 11,200 \text{ ksi}$$

Property	Section Property at Small End	Section Property at Large End
B_2	6.0 in.	6.0 in.
T_2	0.25 in.	0.25 in.
B_3	10.0 in.	24.0 in.
T_3	0.125 in.	0.125 in.
B_4	4.0 in.	4.0 in.
T_4	0.25 in.	0.25 in.
$\bar{Y}$	4.33 in.	10.91 in.
A	3.75 in. ²	5.5 in. ²
I_x	71.26 in. ⁶	497.5 in. ⁴
I_y	5.83 in. ⁴	5.83 in. ⁴
C_w	102.85 in. ⁶	592.46 in. ⁶
J	0.0586 in. ⁶	0.0677 in. ⁴
β_x	5.06 in.	12.33 in.
S_x	16.44 in. ³	45.6 in. ³
S_x	12.57 in. ³	38.0 in. ³

Figure 3. Beam Dimensions and Properties
for Example Calculations

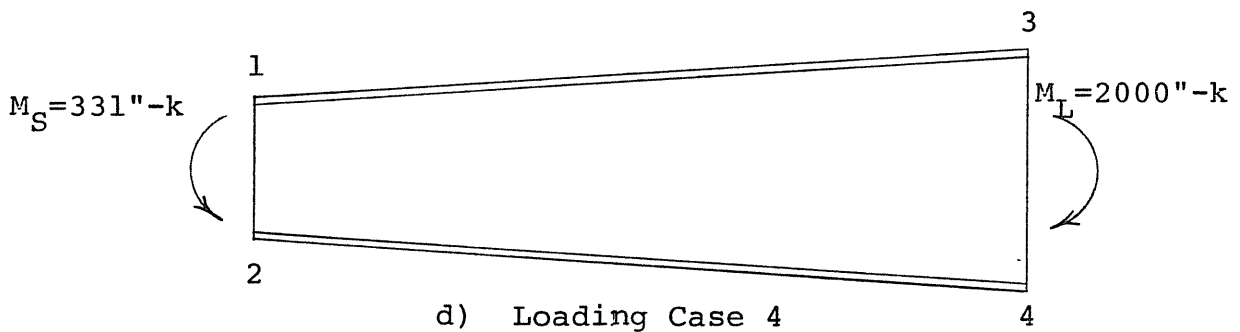
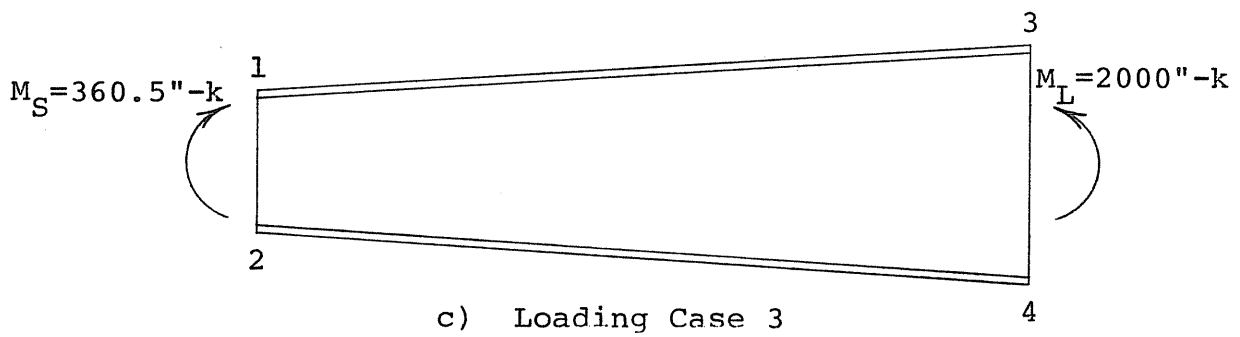
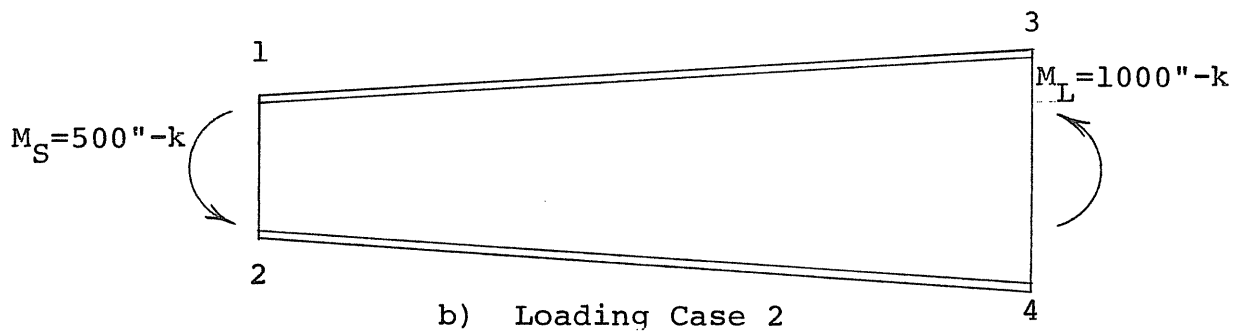
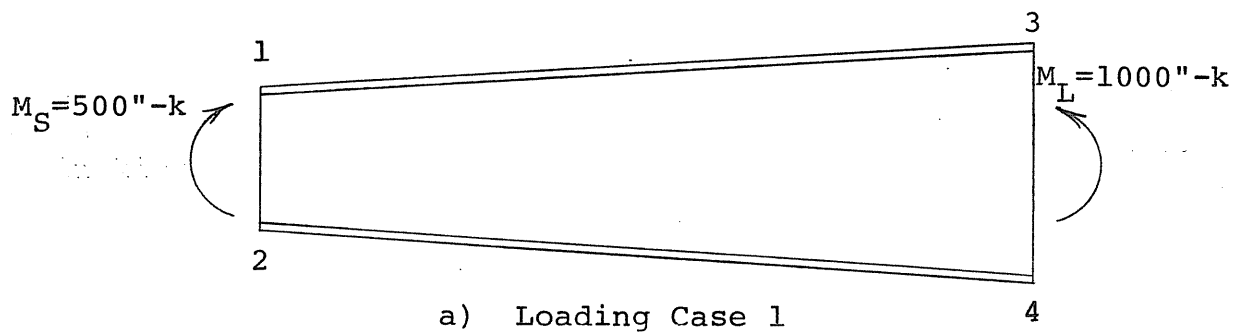


Figure 4. Loading Cases for Example Calculations

LOADING CASE 1

Stresses

$$F_1 = M_S / S_1 = 500 / 16.44 = 30.40 \text{ ksi C}$$

$$F_2 = M_S / S_2 = 500 / 12.57 = 39.78 \text{ ksi T}$$

$$F_3 = M_L / S_3 = 1000 / 45.60 = 21.93 \text{ ksi C}$$

$$F_4 = M_L / S_4 = 1000 / 38.00 = 26.31 \text{ ksi T}$$

Note maximum compressive stress is at 1, therefore, reference end is small end and reference flange is top flange, hence

r = stress ratio for top flange

$$= F_3 / F_1 = 21.93 / 30.4 = 0.721$$

R = moduli ratio for top flange

$$= S_3 / S_1 = 45.6 / 16.44 = 2.77$$

M_e

Basic case moment from equation 2, positive signs.

$$\begin{aligned} M_e &= \frac{\pi^2 (30000) (5.06)}{2 (120)^2} \left\{ 1 + \sqrt{1 + \frac{4}{(5.06)^2} \left(\frac{102.86}{5.83} + \frac{11200 (0.0586) (120)^2}{\pi^2 (30000) (5.83)} \right)} \right\} \\ &= 303.28 \{ 1 + \sqrt{1 + 3.61} \} \\ &= 954.48 \text{ in-kip} \end{aligned}$$

C_a

Using small end properties

$$\begin{aligned} C_a &= 1 - 1.458 (0.1167) \sqrt{\frac{(11200) (0.0586) (120)^2}{(30.000) (102.86)}} \\ &\quad + \frac{44.63 (0.1167) (0.0586)}{5.83} \\ &= 0.754 \end{aligned}$$

C_b

Since $r > -0.40$

$$\begin{aligned} C_b &= 1 - 0.3867(0.721 - 1) + 0.4739(0.721 - 1)^2 + \\ &\quad \frac{0.9074(0.1167)(120)(0.721 - 1)^2}{10.0} \\ &= 1.24 \end{aligned}$$

F_{bc}

Since node 1 is critical

$$\begin{aligned} F_{bc} &= C_a C_b M_e / S_1 = 0.754(1.24)(954.48) / 16.44 \\ &= 54.3 \text{ ksi} > F_y / 2 = 25 \text{ ksi} \end{aligned}$$

Inelastic buckling, CRC Formula

$$F_{bc} = 50.0 - \frac{50.0^2}{4(54.3)} = 38.5 \text{ ksi C}$$

$$\begin{aligned} F_{bt} &= F_{bc} S_1 / S_2 = (38.5)(16.44) / 12.57 \\ &= 50.4 \text{ ksi } T > F_y = 50.0 \text{ ksi} \end{aligned}$$

Tension controls, thus

$$F_{bt} = 50.0 \text{ ksi } T$$

$$F_{bc} = F_y S_2 / S_1 = 50.0(12.57) / 16.44 = 38.2 \text{ ksi C}$$

Critical Final Moments

$$M_S = F_{bc} S_1 = 38.2(16.44) = \underline{628.5 \text{ in-kips}} > 500 \text{ in-kips}$$

$$\begin{aligned} M_L &= M_S rR = 628.5(0.721)(2.77) \\ &= \underline{1255 \text{ in-kips}} > 1000 \text{ in-kips} \end{aligned}$$

Beam is satisfactory for loading

Critical Stresses

$$F_1 = 38.2 \text{ ksi C}$$

$$F_2 = 50.0 \text{ ksi T}$$

$$F_3 = 1255/45.6 = 27.5 \text{ ksi C}$$

$$F_4 = 1255/38.0 = 33.0 \text{ ksi T} < F_y = 50.0 \text{ ksi}$$

LOADING CASE 2

Stresses

$$F_1 = M_S/S_1 = 500/16.44 = 30.40 \text{ ksi T}$$

$$F_2 = M_S/S_2 = 500/12.57 = 39.78 \text{ ksi C}$$

$$F_3 = M_L/S_3 = 1000/45.60 = 21.93 \text{ ksi C}$$

$$F_4 = M_L/S_4 = 1000/38.00 = 26.31 \text{ ksi T}$$

Note maximum compressive stress is at 2. Therefore, reference end is small end and reference flange is bottom flange, hence

r = stress ratio for bottom flange

$$= F_4/F_2 = +26.31/-39.78 = -0.66$$

R = moduli ratio for bottom flange

$$= S_4/S_2 = 38.00/12.57 = 3.02$$

M_e

Basic case moment from equation 2, negative signs

$$M_e = 303.28 (1 - \sqrt{1+3.61})$$

$$= 347.89 \text{ in-kips}$$

C_a

$C_a = 0.754$, same as for loading case 1.

C_b

Since $r < -0.40$

C_{b1} for $r = -0.40$

$$= 1 - 0.3867(-0.4 - 1.0) + 0.4739(-0.4 - 1.0)^2$$

$$+ \frac{0.9074(0.1167)(120)(-0.6 - 1.0)^2}{10}$$

$$= + 4.96$$

C_{b2} for $r = -1.0$

$$\begin{aligned} &= 2.7596 - \frac{2.8152(5.06)}{10} - \frac{0.565(0.1167)(120)}{10} \\ &\quad - \frac{15.653(0.1167)(5.06)}{10} \\ &= -0.508 \end{aligned}$$

Using linear interpolation,

$$\begin{aligned} C_b &= -0.508 + \frac{4.96 + 0.0508}{0.6} (1. - 0.66) \\ &= +2.59 \end{aligned}$$

F_{bc}

Since node 2 is critical

$$\begin{aligned} F_{bc} &= C_a C_b M_e / S_2 = 0.754 (2.59) (347.89) / 12.57 \\ &= 54.0 \text{ ksi} > F_y / 2 = 25 \text{ ksi} \end{aligned}$$

Inelastic buckling, CRC Formula

$$\begin{aligned} F_{bc} &= 50.0 - \frac{50.0^2}{4(54.0)} = 38.4 \text{ ksi C} \\ F_{bt} &= F_{bc} S_2 / S_1 = 38.4 (12.57) / 16.44 \\ &= 29.36 \text{ ksi T} < F_y = 50.0 \text{ ksi} \end{aligned}$$

Critical Moments

$$\begin{aligned} M_S &= F_{bc} S_2 = 38.4 (12.57) = \underline{482.7 \text{ in-kips}} < 500 \text{ in-kips} \\ M_L &= M_S rR = 482.7 (0.66) (3.02) \\ &= \underline{962.1 \text{ in-kips}} < 1000 \text{ in-kips} \end{aligned}$$

Beam is not satisfactory for loading.

Critical Stresses

$$\begin{aligned} F_1 &= 29.36 \text{ ksi T} \\ F_2 &= 38.4 \text{ ksi C} \\ F_3 &= 962.1 / 45.6 = 21.1 \text{ ksi C} \\ F_4 &= 962.1 / 38.0 = 25.3 \text{ ksi T} \end{aligned}$$

LOADING CASE 3

Stresses

$$F_1 = M_S/S_1 = 360.5/16.44 = 21.91 \text{ ksi C}$$

$$F_2 = M_S/S_2 = 500.0/12.57 = 28.68 \text{ ksi T}$$

$$F_3 = M_L/S_3 = 2000.0/45.6 = 43.86 \text{ ksi C}$$

$$F_4 = M_L/S_4 = 2000.0/38.0 = 52.63 \text{ ksi T}$$

Note maximum compressive stress is at 3. Therefore reference end is large and reference flange is top flange, hence

r = stress ratio for top flange

$$= F_1/F_3 = -21.82/-43.86 = +0.50$$

R = moduli ratio for top flange

$$= S_3/S_1 = 45.6/16.44 = 2.77$$

M_e

Basic case moment from equation 2, positive signs

$M_e = 954.48$ in-kips, same as for loading case 1.

C_a

$C_a = 0.754$. Same as for loading case 1.

C_b

Since $r > -0.40$

$$\begin{aligned} C_b &= 1 - 0.386(0.5-1.0) + 0.4739(0.5-1.0)^2 + \\ &\quad \frac{0.9074(0.1167)(120)(0.5-1.0)^2}{24} \\ &= +1.44 \end{aligned}$$

F_{bc}

Since node 3 is critical

$$\begin{aligned} F_{bc} &= C_a C_b M_e R / S_3 \\ &= 0.754(1.44)(954.48)(2.77)/45.6 \\ &= 62.95 \text{ ksi} > \frac{F_y}{2} = 25 \text{ ksi} \end{aligned}$$

Inelastic buckling, CRC Formula

$$F_{bc} = 50.0 - \frac{50.0^2}{4(62.95)} = 40.1 \text{ ksi C}$$

$$F_{bt} = F_{bc} \frac{S_3}{S_4} = 40.1 (45.6)/38.0$$

$$= 48.12 \text{ ksi T} < F_y = 50 \text{ ksi}$$

Critical Moments

$$M_L = F_{bc} S_3 = 40.1 (45.6) = \underline{1828.6 \text{ in-kips}} < 2000 \text{ in-kips}$$

$$M_S = M_L r/R = 1828.6(0.5)/2.77$$

$$= \underline{330 \text{ in-kips}} < 360.5 \text{ in-kips}$$

Beam is not satisfactory for loading

Critical Stresses

$$F_1 = 330/16.44 = 20.1 \text{ ksi C}$$

$$F_2 = 330/12.57 = 26.2 \text{ ksi T}$$

$$F_3 = 40.1 \text{ ksi C}$$

$$F_4 = 48.12 \text{ ksi T}$$

LOADING CASE 4

Stresses

$$F_1 = M_s/S_1 = 331/16.44 = 20.13 \text{ ksi T}$$

$$F_2 = M_s/S_2 = 331/12.57 = 26.33 \text{ ksi C}$$

$$F_3 = M_2/S_3 = 2000/45.6 = 43.86 \text{ ksi T}$$

$$F_4 = M_2/S_4 = 2000/38.0 = 52.63 \text{ ksi C}$$

Note maximum compressive stress is at 4. Therefore, reference end is large end and reference flange is bottom flange, hence

r = stress ratio for bottom flange

$$= F_2/F_4 = -26.33/52.63 = -0.50$$

R = moduli ratio for bottom flange

$$= S_4/S_2 = 38.0/12.57 = 3.02$$

M_e

Basic case moment from equation 2, negative signs

$$M_e = 347.89 \text{ in-kips, same as for loading case 2}$$

C_a

$$C_a = 0.754, \text{ same as for loading case 1 and 2.}$$

C_b

Since $r > -0.40$

$$\begin{aligned} C_b &= 1 - 0.3867(0.5 - 1.0) + 0.4739(0.5 - 1.0)^2 \\ &\quad + 0.9074(0.1167)(120)(0.5 - 1.0)^2/24 \\ &= +1.44 \end{aligned}$$

F_{bc}

Since node 4 is critical,

$$\begin{aligned} F_{bc} &= C_a C_b M_e R / S_4 = 0.754(1.44)(347.84)(3.02)/38 \\ &= 30 \text{ ksi} > \frac{F_y}{2} = 25 \text{ ksi} \end{aligned}$$

Inelastic buckling, CRC Formula

$$F_{bc} = 50.0 - \frac{50.0^2}{4(30)} = 29.2 \text{ ksi C}$$

$$F_{bt} = S_4/S_3 = 29.2 (38.0)/45.6 \\ = 24.3 \text{ ksi T} < F_y = 50 \text{ ksi}$$

Critical Moments

$$M_L = F_{bc} S_4 = 29.2 (38.0) = \underline{1109.6 \text{ in-kips}} < 2000 \text{ in-kips}$$

$$M_S = M_L r/R = 1109.6(0.5)/3.02 \\ = \underline{183.7 \text{ in-kips}} < 331 \text{ in-kips}$$

Beam is not satisfactory for loading

Critical Stresses

$$F_1 = 183.7/16.44 = 11.2 \text{ ksi T}$$

$$F_2 = 183.7/12.57 = 14.6 \text{ ksi C}$$

$$F_3 = 24.3 \text{ ksi T}$$

$$F_4 = 29.2 \text{ ksi C}$$

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APPENDIX
COMPUTER PROGRAM AND EXAMPLE OUTPUT

26


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0033 YOL=B3+HL-YBAL
0034 YOR=BR+HR-YBAR
0035 E0=B2*B2*B1*B1*T1/4./YTL
0036 WIL=YTL*YBL*(EX+B3)**2/YI
0037 WIR=YTL*YBL*(EX+BR)**2/YI
0038 POL=(XIL+YI)/AREA+YOL**2
0039 ROR=(XIR+YI)/AREAR+YOR**2
0040 SL=XIL/YTOL
0041 SF=XIR/YTOR
0042 SBL=XIL/YBAL
0043 SBR=XIR/YBAR
0044 S(1)=SL
0045 S(2)=SBL
0046 S(3)=SR
0047 S(4)=SBR
0048 GAM=YTL*YBL/YI
0049 BXL=(YBAL*(T4*B4**3/12.+B4*T4*YBAL*YBAL)-YTOL*(T2*B2**3/12.+B2*T2*
1YTOL*YTOL)-B2*B2*B1*T1*(YTCL/2.-B1/4.)-2.*B1*T1*(YTOL**3-1.5*B1*YT
20L*YTOL+B1*B1*YTOL-B1*B1*B1/4.)+YBAL**4*T3/4.-YTOL**4*T3/4.)/XIL+2
3.*YOL
0050 BXR=(YBAR*(T4*B4**3/12.+B4*T4*YBAR*YBAR)-YTOR*(T2*B2**3/12.+B2*T2*
1YTOR*YTOR)-B2*B2*B1*T1*(YTOR/2.-B1/4.)-2.*B1*T1*(YTOR**3-1.5*B1*YT
20R*YTOR+B1*B1*YTOR-B1*B1*B1/4.)+YBAR**4*T3/4.-YTOR**4*T3/4.)/XIP+2
3.*YOR

```

C CHECKING SECTION LIMITATIONS

```

0051 DWT=B3/B2
0052 DMB=B3/B4
0053 XLB3=XL/B3
0054 B2T2=B2/T2
0055 B4T4=B4/T4
0056 R1=(YTL/YBL)*(ALPHA*XL/B3)
0057 R2=YTL/YBL
0058 IF(DWT.LT.1.5.OR.DMB.LT.1.5.OR.DWT.GT.3.0.OR.DMB.GT.3.0.OR.XLB3.GT
1.24.OR.B2T2.LT.15.0.OR.B4T4.LT.15.0.OR.B2T2.GT.50.0.OR.B4T4.GT.5
20.0.OR.B3.LT.6.0.OR.B3.GT.24.0.OP.B2.LT.3.0.OP.B2.GT.12.0.OP.B4.LT
4.3.0.OP.B4.GT.12.0.OP.T2.LT.0.1875.OR.T2.GT.0.75.OP.T4.LT.0.1875.0
SR.T4.GT.0.75.OP.R1.GT.1.30.CR.R2.GT.2.50)GO TO 750
GO TO 171

```

C OUTPUT OF SECTION DATA

```

0060 750 WRITE(6,114)B1,T1,B2,T2,B3,T3,B4,T4,XL,ALPHA,FY
0061 114 FORMAT(1H0,/,/, SECTION DOES NOT MEET SPECIFIED LIMITATIONS',/,/,
1 DIMENSIONS OF CROSS SECTION',/,/,3X,'R1 =',F9.4,' IN',3X,'T1 =
2',F7.4,' IN',/,/,3X,'B2 =',F9.4,' IN',3X,'T2 =',F7.4,' IN',/,/,
.33X,'B3 =',F9.4,' IN',3X,'T3 =',F7.4,' IN',/,/,3X,'B4 =',F9.4,
4' IN',3X,'T4 =',F7.4,' IN',/,/,3X,'LENGTH =',F10.2,' IN',/,/,3X,'A
SLPHA =',F8.4,/,/,2X,'FY =',F7.2,' KSI')
GO TO 170
0062 171 WRITE(6,113)B1,T1,B2,T2,B3,T3,B4,T4,XL,ALPHA,FY
0063 113 FORMAT(1H0,/,/ DIMENSIONS OF CROSS SECTION',/,/
13X,'B1 =',F9.4,' IN',3X,'T1 =',F7.4,' IN',/,/
13X,'B2 =',F9.4,' IN',3X,'T2 =',F7.4,' IN',/,/
13X,'B3 =',F9.4,' IN',3X,'T3 =',F7.4,' IN',/,/
13X,'B4 =',F9.4,' IN',3X,'T4 =',F7.4,' IN',/,/
13X,'LENGTH=',F10.2,' IN',/,/,3X,'ALPHA =',F8.4,/,/,2X,'FY =',F7.

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```

0065      12.0 KSI')
0066      170 WRITE(6,111)ROL,ROR,YOL,YOR,YTOL,YTOR
0066      111 FORMAT(
0066          ///,10X,'LEFT END SECTION PROPERTIES',20X,'PICH
0066          2T END SECTION PROPERTIES',//,7X,'RO' =,F11.4,' IN',22X,'RO' =
0066          2',F10.4,' IN',//,7X,'YO' =,F10.4,' IN',22X,'YO' =,F10.4,'
0066          3IN',//,7X,'YBAR' =,F10.4,' IN. FROM TOP',13X,'YBAR' =,F10.4,' I
0066          IN. FROM TOP')
0067      WRITE(6,103)YBAL,YBAR,AREA,AREAR,XIL,XIR
0068      103 FORMAT(/,7X,'YBAR' =,F10.4,' IN. FROM BOTTOM',11X,'YBAR' =,F10.4,
0068          1' IN. FROM BOTTOM',//,7X,'AREA' =,F10.4,' IN**2',20X,'AREA' =,F1
0068          20.4,' IN**2',//,7X,'IX' =,F10.4,' IN**4',20X,'IX' =,F10.4,'
0068          3IN**4')
0069      WRITE(6,73)YI,YI,WIL,WIR,TJL,TJR,BXL,BXR,S(1),S(3),S(2),S(4)
0070      73 FORMAT(/,7X,'YI' =,F10.4,' IN**4',20X,'YI' =,F10.4,' IN**4,
0070          1',//,7X,'CW' =,F10.4,' IN**6',20X,'CW' =,F10.4,' IN**6',//,7X
0070          2',J' =,F10.4,' IN**4',20X,'J' =,F10.4,' IN**4',//,7X,'BX
0070          3' =,F10.4,' IN',22X,'BX' =,F10.4,' IN',//,7X,'SEC. MOD.' =,F
0070          410.4,' IN**3 TOP',12X,'SEC. MOD.' =,F10.4,' IN**3 TOP',//,7X,'SEC.
0070          5 MOD.' =,F10.4,' IN**3 BOTTOM',9X,'SEC. MOD.' =,F10.4,' IN**3 BOT
0070          6OM')
0071      WRITE(6,75)XMS,XML
0072      75 FORMAT(/,7X,'MOMENT' =,F10.2,' K-IN',19X,'MOMENT' =,F10.2,' K-IN
0072          1.')
```

CALCULATION OF STRESSES AT FLANGE TIPS

```

0073      F(1)=-XMS/S(1)
0074      F(2)=XMS/S(2)
0075      F(3)=XML/S(3)
0076      F(4)=-XML/S(4)
0077      WRITE(6,2001)
0078      WRITE(6,2000)
0079      WRITE(6,112)F(1),F(2),F(3),F(4)
0080      112 FORMAT(/,1X,'STRESS AND MOMENT RESULTS',//,3X,'STRESS AT LEFT TO
0080          IP' =,F10.2,' KSI',10X,'STRESS AT LEFT BOTTOM' =,F9.2,' KSI',//,3
0080          2X,'STRESS AT RIGHT TOP' =,F10.2,' KSI',10X,'STRESS AT RIGHT BOTTOM
0080          3' =,F9.2,' KSI')
0081      105 I=1
0082      J=1
0083      180 FMIN=F(J)
0084      106 I=I+1
0085      107 IF(I,LE,4)GO TO 108
0086      GO TO 109
0087      108 IF(FMIN,LT,F(I))GO TO 106
0088      J=I
0089      GO TO 180
0090      109 WRITE(6,110)J,FMIN
0091      110 FORMAT(/,3X,'NODE WITH MAX. COMPR. STRESS' =,I3,//,3X,'MAX. COMP.
0091          1 STRESS' =,F10.2,' KSI')
0092      C
0093      C
0094      C
0095      C
0096      C
0097      C
0098      C
0099      C
0100      C
0101      C
0102      C
0103      C
0104      C
0105      C
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0963      C
0964      C
0965      C
0966      C
0967      C
0968      C
0969      C
0970      C
0971      C
0972      C
0973      C
0974      C
0975      C
0976      C
0977      C
0978      C
0979      C
0980      C
0981      C
0982      C
0983      C
0984      C
0985      C
0986      C
0987      C
0988      C
0989      C
0990      C
0991      C
0992      C
0993      C
0994      C
0995      C
0996      C
0997      C
0998      C
0999      C
1000      C
```

```

0096      1XL**2/(PI**2*(E*VI))**0.5)
0097 S10 WRITE(6,120) CRM
        120 FORMAT(/,/,3X,'CRITICAL MOMENT BASIC CASE =',F10.2,' K-IN.')
C
C      CALCULATION OF CA
C
0098      CA=1.0-1.4580*ALPHA*(G*TJL*XL**2/(E*WIL))**0.5+44.6328*ALPHA*TJL/V
        11
0099      IF(J.EQ.1.OR.J.EQ.3)GO TO 520
0100      R=S(4)/S(2)
0101      GO TO 530
0102      520 R=S(3)/S(1)
C
C      CALCULATION OF CB
C
0103      530 IF(J.EQ.1.OR.J.EQ.2)GO TO 540
0104      IF(J.EQ.3)GO TO 550
0105      RF=F(2)/F(4)
0106      GO TO 560
0107      550 RF=F(1)/F(3)
0108      GO TO 560
0109      540 RF=F(4)/F(2)
0110      IF(J.EQ.1)RF=F(3)/F(1)
C
0111      560 WRITE(6,130) R,RF
0112      130 FORMAT(/,/,3X,'MODULAR RATIO REF. FLANGE =',F10.2,'/,3X,'STRESS RAT
        110 REF. FLANGE =' ,F10.4)
C
0113      565 IF(RF+0.4)570,580,580
C
C      CALCULATION OF CB IF RF IS GREATER THAN -0.4
C
0114      580 CB=1.-0.3867*(PF-1.)+0.4739*(RF-1.)**2+0.9074*ALPHA*
        1XL*(RF-1.)**2/B3
0115      IF(J.EQ.3.OR.J.EQ.4)GO TO 590
0116      GO TO 630
0117      590 CB=1.-0.3867*(RF-1.)+0.4739*(RF-1.)**2+0.9074*ALPHA*
        1XL*(RF-1.)**2/BR
        GO TO 630
0118
C
C      CALCULATION OF CB IF RF IS LESS THAN -0.4
C
0119      570 CB=1.-0.3867*(-0.4-1.)+0.4739*(-0.4-1.)**2+0.9074*ALPHA*XL*
        1*(-0.4-1.)**2/B3
0120      IF(J.EQ.3.OR.J.EQ.4)GO TO 600
0121      GO TO 615
0122      600 CB=1.-0.3867*(-0.4-1.)+0.4739*(-0.4-1.)**2+0.9074*ALPHA*XL*
        1*(-0.4-1.)**2/BR
        IF(J.EQ.3.OR.J.EQ.4)GO TO 610
0123      615 CB2=2.7596-2.8152*BXL/B3-0.6562*ALPHA*XL/B3-15.653*ALPHA*BXL/B3
0124      GO TO 620
0125      610 CB2=2.7684+1.2025*ALPHA*XL/BR-2.2686*BXR/BR-22.0274*ALPHA*BXR/BR
0126      620 CB=CB2+(CB1-CB2)*(1.+RF)/0.6
0127      630 WRITE(6,140)CA,CB
0128      140 FORMAT(/,/,3X,'CA =',F10.4,'CB =',F10.4)
0129
C
C      CALCULATION OF MAX. COMPRESSIVE STRESS AT REFERENCE END

```

```
C
0130 IF(J.EQ.3.OR.J.EQ.4)GO TO 700
0131 IF(F(1).LT.0.0) GO TO 900
0132 S(5)=S(2)
0133 S(6)=S(1)
0134 GO TO 1000
0135 900 S(5)=S(1)
0136 S(6)=S(2)
0137 GO TO 1000
0138 700 IF(F(3).LT.0.0) GO TO 950
0139 S(5)=S(4)
0140 S(6)=S(3)
0141 GO TO 1200
0142 950 S(5)=S(3)
0143 S(6)=S(4)
C
C MAX. COMPRESSIVE STRESS LARGE END REFERENCE
C
0144 1200 FBC=CA*CB*P*CRM/S(5)
0145 GO TO 1250
C
C MAX. COMPRESSIVE STRESS SMALL END REFERENCE
C
0146 1000 FBC=CA*CB*CRM/S(5)
C
C MODIFICATION OF FBC USING CRC FORMULA, IF NECESSARY
C
0147 1250 FALL=0.5*FY
0148 FBC=ABS(FBC)
0149 IF(FBC.LT.FALL)GO TO 1400
0150 FBC=FY*(1.-FY/(4.*FBC))
C
C CHECK TO SEE IF YIELDING GOVERNS
C
0151 1400 FBT=FBC*S(5)/S(6)
0152 IF(FBT.LT.FY)GO TO 1450
0153 FBT=FY
C
C MODIFICATION OF FBC IF YIELDING GOVERNS
C
0154 FBC=FBT*S(6)/S(5)
0155 GO TO 800
0156 1450 WRITE(6,1410)FBC
0157 1410 FORMAT(/,/,3X,'GOVERNING STRESS AT FAILURE =',F7.2,' KSI C')
0158 WRITE(6,1411)J
0159 GO TO 812
0160 800 IF(J.EQ.1.OR.J.EQ.3)GO TO 811
0161 K=J-1
0162 GO TO 830
0163 811 K=J+1
0164 830 WRITE(6,810)FBT
0165 810 FORMAT(/,/,3X,'GOVERNING STRESS AT FAILURE =',F7.2,' KSI T')
0166 WRITE(6,1411)K
0167 1411 FORMAT(/,/,3X,'LOCATION OF GOVERNING STRESS =',I3)
0168 812 IF(J.EQ.3.OR.J.EQ.4)GO TO 200
C
C CALCULATION OF STRESSES AND MOMENTS AT FAILURE, SMALL END REFERENCE
C
```

```
0169 MCRS=FBC*S(5)
0170 F1=MCRS/S(1)
0171 F2=MCRS/S(2)
0172 XCRL=MCFS*RF#R
0173 MCRL=ABS(XCRL)
0174 F3=MCRL/S(3)
0175 F4=MCRL/S(4)
0176 IF(J.EQ.2)GO TO 201
0177 IF(PF.LT.0.0)GO TO 301
0178 WRITE(6,400)F1,F3,F2,F4
0179 GO TO 815
0180 301 WRITE(6,401)F1,F3,F2,F4
0181 GO TO 815
0182 201 IF(RF.LT.0.0)GO TO 302
0183 WRITE(6,403)F1,F3,F2,F4
0184 GO TO 815
0185 302 WRITE(6,404)F1,F3,F2,F4
0186 GO TO 815

C
C      CALCULATION OF STRESSES AND MOMENTS AT FAILURE,LARGE END REFERENCE
C
0187 200 MCRL=FBC*S(5)
0188 F3=MCRL/S(3)
0189 F4=MCRL/S(4)
0190 XCRL=MCRL*RF#R
0191 MCRS=ABS(XCRL)
0192 F1=MCRS/S(1)
0193 F2=MCRS/S(2)
0194 IF(J.EQ.4)GO TO 304
0195 IF(PF.LT.0.0)GO TO 303
0196 WRITE(6,400)F1,F3,F2,F4
0197 400 FORMAT(/,3X,'STRESSES AT FAILURE',/,7X,'LOCATION 1 ',F10.2,' KS
11 C',20X,'LOCATION 3 ',F10.2,' KSI C',/,7X,'LOCATION 2 ',F10.2,
2' KSI T',20X,'LOCATION 4 ',F10.2,' KSI T')
GO TO 815
0198 303 WRITE(6,404)F1,F3,F2,F4
0199 404 FORMAT(/,3X,'STRESSES AT FAILURE',/,7X,'LOCATION 1 ',F10.2,' KS
200 11 T',20X,'LOCATION 3 ',F10.2,' KSI C',/,7X,'LOCATION 2 ',F10.2,
201 2' KSI C',20X,'LOCATION 4 ',F10.2,' KSI T')
GO TO 815
0202 304 IF(PF.LT.0.0)GO TO 305
0203 WRITE(6,403)F1,F3,F2,F4
0204 403 FORMAT(/,3X,'STRESSES AT FAILURE',/,7X,'LOCATION 1 ',F10.2,' KS
11 T',20X,'LOCATION 3 ',F10.2,' KSI T',/,7X,'LOCATION 2 ',F10.2,
2' KSI C',20X,'LOCATION 4 ',F10.2,' KSI C')
GO TO 815
0205 305 WRITE(6,401)F1,F3,F2,F4
0206 401 FORMAT(/,3X,'STRESSES AT FAILURE',/,7X,'LOCATION 1 ',F10.2,' KS
11 C',20X,'LOCATION 3 ',F10.2,' KSI T',/,7X,'LOCATION 2 ',F10.2,
2' KSI T',20X,'LOCATION 4 ',F10.2,' KSI C')
0208 815 WRITE(6,402)MCRS,MCRL
0209 402 FORMAT(/,3X,'CRITICAL MOMENTS AT FAILURE',/,7X,'SMALL END ',F10
1.2,' IN-K',20X,'LARGE END ',F10.2,' IN-K')
GO TO 999
0210 55 STOP
0211 END
0212
```

OPTIONS IN EFFECT NOTERM, ID, EBCDIC, SOURCE, NOLIST, NODECK, LOAD, NOMAP, NOTEST
OPTIONS IN EFFECT NAME = MAIN, LINECNT = 60
STATISTICS SOURCE STATEMENTS = 212, PROGRAM SIZE = 9784
STATISTICS NO DIAGNOSTICS GENERATED

MODULE MAP

CONTROL SECTION				ENTRY							
NAME	ORIGIN	LENGTH		NAME	LOCATION	NAME	LOCATION	NAME	LOCATION	NAME	LOCATION
MAIN	00	2638									
IHOFRXPR*	2638	4A4		FRXPR#	2638						
IHOECOMH*	2AE0	E30		IBCOM#	2B14	FDIOCS#	2BD0	INTSWTCH	3858		
FIDAP# *	3910	624		SEQDASD	430A						
IHOCCMH2*	3F38	9A5									
IHOFCVTH*	48E0	CEA		ADCON#	48E0	FCVAOUTP	494C	FCVLOUTP	4964	FCVZOUTP	497C
				FCVIOUTP	4994	FCVEOUTP	49CC	FCVCOUTP	49CC	ADCONI#	50D0
				ADCONO#	50EC	INT6SWCH	55C9				
				ARITH#	55D0	ADJSWTCH	5B64				
IHOEFNTH*	55D0	800		FIOCS#	5DD0	FIOCSBEP	5DD6				
IHOEFICS*	5DD0	118C									
IHOFIOS2*	6F60	642		IHS\$EXP	75A8	EXP	75A8				
IHOSEXP *	75A8	258		IHSALOG	7800	ALOG	7800	LOG	7800		
IHOISLGN *	7800	244		ERRMON	7A48	IHOERRE	7A60				
IHOERRM *	7A48	624									
IHOUDPT *	8070	338		FQCONI#	83A8						
IHOFCONI*	83A8	416		FQCONO#	87C0						
IHOFCONO*	87C0	888		IHO TRCH	9078	ERRTRA	9080				
IHOETRCH*	9078	2AE									
IHOUATBL*	9328	638		FTEN#	9960						
IHOFTEN *	9960	220									

ENTRY ADDRESS 00

TOTAL LENGTH 9880

***F0RTGCLG DOES NOT EXIST BUT HAS BEEN ADDED TO DATA SET
 AUTHORIZATION CODE IS 0.

EXAMPLE PROBLEM CASE 1

SECTION DOES NOT MEET SPECIFIED LIMITATIONS

DIMENSIONS OF CROSS SECTION

B1 = 0.0 IN T1 = 0.0 IN
 B2 = 6.0000 IN T2 = 0.2500 IN
 B3 = 10.0000 IN T3 = 0.1250 IN
 B4 = 4.0000 IN T4 = 0.2500 IN

LENGTH = 120.00 IN

ALPHA = 0.1167

FY = 50.00 KSI

LEFT END SECTION PROPERTIES

RO = 24.7510 IN.
 YO = 2.0476 IN.
 YBAR = 4.3333 IN. FROM TOP
 YBAR = 5.6667 IN. FROM BOTTOM
 AREA = 3.7500 IN**2
 IX = 71.2630 IN**4
 IY = 5.8333 IN**4
 CW = 102.8571 IN**6
 J = 0.0586 IN**4
 BX = 9.0659 IN.
 SEC. MOD. = 16.4453 IN**3 TOP
 SEC. MOD. = 12.9798 IN**3 BOTTOM

MOMENT = 500.00 K-IN.

RIGHT END SECTION PROPERTIES

RO = 120.9223 IN.
 YO = 5.4234 IN.
 YBAR = 10.9091 IN. FROM TOP
 YBAR = 13.0909 IN. FROM BOTTOM
 AREA = 5.5000 IN**2
 IX = 497.4683 IN**4
 IY = 5.8333 IN**4
 CW = 592.4583 IN**6
 J = 0.0677 IN**4
 BX = 12.3334 IN.
 SEC. MOD. = 45.6012 IN**3 TOP
 SEC. MOD. = 38.0010 IN**3 BOTTOM

MOMENT = -1000.00 K-IN.

EXAMPLE PROBLEM CASE 1

STRESS AND MOMENT RESULTS

STRESS AT LEFT TOP = -30.40 KSI STRESS AT LEFT BOTTOM = 39.76 KSI
STRESS AT RIGHT TOP = -21.93 KSI STRESS AT RIGHT BOTTOM = 26.32 KSI

NODE WITH MAX. COMPR. STRESS = 1

MAX. COMP. STRESS = -30.40 KSI

CRITICAL MOMENT BASIC CASE = 955.48 K-IN.

MODULAR RATIO REF. FLANGE = 2.77

STRESS RATIO REF. FLANGE = 0.7213

CA = 0.7346 CB = 1.2433

GOVERNING STRESS AT FAILURE = 50.00 KSI T

LOCATION OF GOVERNING STRESS = 2

STRESSES AT FAILURE

LOCATION 1 38.24 KSI C LOCATION 3 27.58 KSI C
LOCATION 2 50.00 KSI T LOCATION 4 33.09 KSI T

CRITICAL MOMENTS AT FAILURE

SMALL END 628.79 IN-K LARGE END 1257.58 IN-K

EXAMPLE PROBLEM CASE 2

SECTION DOES NOT MEET SPECIFIED LIMITATIONS

DIMENSIONS OF CROSS SECTION

B1 = 0.0 IN T1 = 0.0 IN
 B2 = 6.0000 IN T2 = 0.2500 IN
 B3 = 10.0000 IN T3 = 0.1250 IN
 B4 = 4.0000 IN T4 = 0.2500 IN

LENGTH = 120.00 IN

ALPHA = 0.1167

FY = 50.00 KSI

LEFT END SECTION PROPERTIES

RO = 24.7518 IN.
 YO = 2.0476 IN.
 YBAR = 4.3333 IN. FROM TOP
 YBAR = 5.6667 IN. FROM BOTTOM
 AREA = 3.7500 IN**2
 IX = 71.2630 IN**4
 IY = 5.8333 IN**4
 CW = 102.2571 IN**6
 J = 0.0586 IN**4
 BX = 5.0658 IN.
 SEC. MOD. = 16.4453 IN**3 TOP
 SEC. MOD. = 12.5758 IN**3 BOTTOM

MOMENT = -500.00 K-IN.

RIGHT END SECTION PROPERTIES

RO = 120.9223 IN.
 YO = 5.4234 IN.
 YBAR = 10.9091 IN. FROM TOP
 YBAR = 13.0909 IN. FROM BOTTOM
 AREA = 5.5000 IN**2
 IX = 497.4683 IN**4
 IY = 5.8333 IN**4
 CW = 592.4583 IN**6
 J = 0.0677 IN**4
 BX = 12.3334 IN.
 SEC. MOD. = 45.6012 IN**3 TOP
 SEC. MOD. = 38.0010 IN**3 BOTTOM

MOMENT = -1000.00 K-IN.

EXAMPLE PROBLEM CASE 2'

STRESS AND MOMENT RESULTS

STRESS AT LEFT TOP = 30.40 KSI STRESS AT LEFT BOTTOM = -39.76 KSI
 STRESS AT RIGHT TOP = -21.93 KSI STRESS AT RIGHT BOTTOM = 26.32 KSI

NODE WITH MAX. COMPR. STRESS = 2

MAX. COMP. STRESS = -39.76 KSI

CRITICAL MOMENT BASIC CASE = -347.87 K-IN.

MODULAR RATIO REF. FLANGE = 3.02

STRESS RATIO REF. FLANGE = -0.6619

CA = 0.7546 CB = 2.5726

GOVERNING STRESS AT FAILURE = 30.36 KSI C

LOCATION OF GOVERNING STRESS = 2

STRESSES AT FAILURE

LOCATION 1	29.34 KSI T	LOCATION 3	21.16 KSI C
LOCATION 2	30.36 KSI C	LOCATION 4	25.39 KSI T

CRITICAL MOMENTS AT FAILURE

SMALL END	482.43 IN-K	LARGE END	964.85 IN-K
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EXAMPLE PROBLEM CASE 3

SECTION DOES NOT MEET SPECIFIED LIMITATIONS

DIMENSIONS OF CROSS SECTION

B1 = 0.0 IN T1 = 0.0 IN
 B2 = 6.0000 IN T2 = 0.2500 IN
 B3 = 10.0000 IN T3 = 0.1250 IN
 B4 = 4.0000 IN T4 = 0.2500 IN

LENGTH = 120.00 IN

ALPHA = 0.1167

FY = 50.00 KSI

30

LEFT END SECTION PROPERTIES

RO = 24.7518 IN.
 YO = 2.0476 IN.
 YBAR = 4.3333 IN. FROM TOP
 YBAR = 5.6667 IN. FROM BOTTOM
 AREA = 3.7500 IN**2
 IX = 71.2630 IN**4
 IY = 5.8333 IN**4
 CW = 102.2571 IN**6
 J = 0.0586 IN**4
 BX = 5.0658 IN.

SEC. MOD. = 16.4453 IN**3 TOP
 SEC. MOD. = 12.5758 IN**3 BOTTOM

MOMENT = 360.50 K-IN.

RIGHT END SECTION PROPERTIES

RO = 120.9223 IN.
 YO = 5.4234 IN.
 YBAR = 10.9091 IN. FROM TOP
 YBAR = 13.0909 IN. FROM BOTTOM
 AREA = 5.5000 IN**2
 IX = 497.4683 IN**4
 IY = 5.8333 IN**4
 CW = 592.4583 IN**6
 J = 0.0677 IN**4
 BX = 12.3334 IN.

SEC. MOD. = 45.6012 IN**3 TOP
 SEC. MOD. = 38.0010 IN**3 BOTTOM

MOMENT = -2000.00 K-IN.

EXAMPLE PROBLEM CASE 3'

STRESS AND MOMENT RESULTS

STRESS AT LEFT TOP = -21.92 KSI STRESS AT LEFT BOTTOM = 28.67 KSI
STRESS AT RIGHT TOP = -43.86 KSI STRESS AT RIGHT BOTTOM = 52.63 KSI

NODE WITH MAX. COMPR. STRESS = 3

MAX. COMP. STRESS = -43.86 KSI

CRITICAL MOMENT BASIC CASE = 955.48 K-IN.

MODULAR RATIO REF. FLANGE = 2.77

STRESS RATIO REF. FLANGE = 0.4998

CA = 0.7546 CB = 1.4444

GOVERNING STRESS AT FAILURE = 40.13 KSI C

LOCATION OF GOVERNING STRESS = 3

STRESSES AT FAILURE

LOCATION 1	20.06 KSI C	LOCATION 3	40.13 KSI C
LOCATION 2	26.23 KSI T	LOCATION 4	48.16 KSI T

CRITICAL MOMENTS AT FAILURE

SMALL END	329.86 IN-K	LARGE END	1830.02 IN-K
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EXAMPLE PROBLEM CASE 4

SECTION DOES NOT MEET SPECIFIED LIMITATIONS

DIMENSIONS OF CROSS SECTION

B1 = 0.0 IN T1 = 0.0 IN

B2 = 6.0000 IN T2 = 0.2500 IN

B3 = 10.0000 IN T3 = 0.1250 IN

B4 = 4.0000 IN T4 = 0.2500 IN

LENGTH = 120.00 IN

ALPHA = 0.1167

FY = 50.00 KSI

LEFT END SECTION PROPERTIES

RO = 24.7518 IN.

YO = 2.0476 IN.

YBAR = 4.3333 IN. FROM TOP

YBAR = 5.6667 IN. FROM BOTTOM

AREA = 3.7500 IN²

IX = 71.2630 IN⁴

IY = 5.8333 IN⁴

CW = 102.8571 IN⁶

J = 0.0586 IN⁴

BX = 5.0658 IN.

SEC. MOD. = 16.4453 IN³ TOP

SEC. MOD. = 12.5758 IN³ BOTTOM

MOMENT = -331.00 K-IN.

RIGHT END SECTION PROPERTIES

RO = 120.9223 IN.

YO = 5.4234 IN.

YBAR = 10.9091 IN. FROM TOP

YBAR = 13.0909 IN. FROM BOTTOM

AREA = 5.3000 IN²

IX = 497.4683 IN⁴

IY = 5.8333 IN⁴

CW = 592.4583 IN⁶

J = 0.0677 IN⁴

BX = 12.3334 IN.

SEC. MOD. = 45.6012 IN³ TOP

SEC. MOD. = 38.0010 IN³ BOTTOM

MOMENT = 2000.00 K-IN.

EXAMPLE PROBLEM CASE 4

STRESS AND MOMENT RESULTS

STRESS AT LEFT TOP = 20.13 KSI STRESS AT LEFT BOTTOM = -26.32 KSI
 STRESS AT RIGHT TOP = 43.86 KSI STRESS AT RIGHT BOTTOM = -52.63 KSI

NODE WITH MAX. COMPR. STRESS = 4

MAX. COMP. STRESS = -52.63 KSI

CRITICAL MOMENT BASIC CASE = -347.87 K-IN.

MODULAR RATIO REF. FLANGE = 3.02

STRESS RATIO REF. FLANGE = 0.5001

CA = 0.7546 CB = 1.4440

GOVERNING STRESS AT FAILURE = 29.27 KSI C

LOCATION OF GOVERNING STRESS = 4

STRESSES AT FAILURE

LOCATION 1	11.19 KSI T	LOCATION 3	24.39 KSI T
LOCATION 2	14.64 KSI C	LOCATION 4	29.27 KSI C

CRITICAL MOMENTS AT FAILURE

SMALL END	184.05 IN-K	LARGE END	1112.11 IN-K
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